Concurrent Models of Computation

Edward A. Lee
Professor, UC Berkeley
Ptolemy Project
CHESS: Center for Hybrid and Embedded Software Systems

HP Workshop on Advanced Software Technologies
July 20-22
HP Labs, Palo Alto, CA

Standard Software Abstraction
(20-th Century Computation)

\[ f : \text{State} \rightarrow \text{State} \]

• Time is irrelevant
• All actions are ordered
Standard Software Abstraction: Processes or Threads

Infinite sequences of state transformations are called “processes” or “threads”.

The operating system (typically) provides:
- suspend/resume
- mutual exclusion
- semaphores

Standard Software Abstraction: Concurrency via Interacting Threads

Potential for race conditions, deadlock, and livelock severely compromises software reliability.

These methods date back to the 1960’s (Dijkstra).
A Stake in the Ground

Nontrivial concurrent programs based on processes, threads, semaphores, and mutexes are incomprehensible to humans.

- No amount of process improvement is going to change this.
  - the human brain doesn’t work this way.
- Formal methods may help
  - scalability?
  - understandability?
- Better concurrency abstractions will help more

A Story: Ptolemy Project Code Review
Ptolemy Project Code Review
A Typical Story

- Code review discovers that a method needs to be synchronized to ensure that multiple threads do not reverse each other’s actions.
- No problems had been detected in 4 years of using the code.
- Three days after making the change, users started reporting deadlocks caused by the new mutex.
- Analysis and correction of the deadlock is hard.

- But code review successfully identified the flaw.

```java
public synchronized void addChangeListener(ChangeListener listener) {
    NamedObject container = (NamedObject) getContainer();
    if (container == null) {
        container.addChangeListener(listener);
    } else {
        if (_changeListeners == null) {
            _changeListeners = new LinkedList();
            _changeListeners.add(0, listener);
        } else if (_changeListeners.contains(listener)) {
            _changeListeners.add(0, listener);
        }
    }
}
```

Code that had been in use for four years, central to Ptolemy II, with an extensive test suite, design reviewed to yellow, then code reviewed to green in 2000, causes a deadlock during a demo on April 26, 2004.

Code Review Doesn’t Always Work
Another Typical Story

```java
public final class CrossRefList implements Serializable {

protected class CrossRef implements Serializable {

    private synchronized Object _farContainer() {
        if (_far != null) return _far._nearContainer();
        else return null;
    }

    ...
}

protected synchronized Object _nearContainer() {
    // NOTE: It is essential that this method not be synchronized, since it is called by _farContainer(), which is. Having it synchronized can lead to deadlock. Fortunately, it is an atomic action, so it need not be synchronized.
    return _container;
}
```

Code that had been in use for four years, central to Ptolemy II, with an extensive test suite, design reviewed to yellow, then code reviewed to green in 2000, causes a deadlock during a demo on April 26, 2004.
And Doubts Remain

/**
 * CrossRefList is a list that maintains pointers to other CrossRefLists.
 *
 * @author Geroncio Galicia, Contributor: Edward A. Lee
 * @version $Id: CrossRefList.java,v 1.78 2004/04/29 14:50:00 eal Exp $
 * @since Ptolemy II 0.2
 * @Pt.ProposedRating Green (eal)
 * @Pt.AcceptedRating Green (bart)
 */
public final class CrossRefList implements Serializable {
    protected class CrossRef implements Serializable {
        private synchronized void _dissociate() {
            _unlink(); // Remove this.
            // NOTE: Deadlock risk here! If _far is waiting
            // on a lock to this CrossRef, then we will get
            // deadlock. However, this will only happen if
            // we have two threads simultaneously modifying a
            // model. At the moment (4/29/04), we have no
            // mechanism for doing that without first
            // acquiring write permission the workspace().
            // Two threads cannot simultaneously hold that
            // write access.
            if (_far != null) _far._unlink(); // Remove far
        }
    }
}

What it Feels Like to Use the synchronized Keyword in Java

Safety of this code depends on policies maintained by entirely unconnected classes. The language and synchronization mechanisms provide no way to talk about these systemwide properties.
Diagnosis: Interacting Processes are Not Compositional

An aggregation of processes is not a process (a total order of external interactions). What is it? Many software failures are due to this ill-defined composition.

Distributed Version of 20-th Century Computation

Force-fitting the sequential abstraction onto parallel hardware.
Combining Processes and RPC – Split-Phase Execution, Futures, Asynchronous Method Calls, Callbacks, ...

These methods are at least as incomprehensible as concurrent threads or processes.

“asynchronous” procedure call

Model Used in Wireless Sensor Nets
No Threads: nesC and TinyOS

Typical usage pattern:
- hardware interrupt signals an event.
- event handler posts a task.
- tasks are executed when machine is idle.
- tasks execute atomically w.r.t. one another.
- tasks can invoke commands and signal events.
- hardware interrupts can interrupt tasks.
- exactly one monitor, implemented by disabling interrupts.

Command implementers can invoke other commands or post tasks, but do not trigger events.
Ptolemy II: Framework for Experimenting with Alternative Concurrent Models of Computation

Basic Ptolemy II infrastructure:

- Director from a library defines component interaction semantics
- Large, domain-polymorphic component library
- Visual editor supporting an abstract syntax

The Basic Abstract Syntax

- Actors
- Attributes on actors (parameters)
- Ports in actors
- Links between ports
- Width on links (channels)
- Hierarchy

Concrete syntaxes:
- XML
- Visual pictures
- Actor languages (Cal, StreamIT, …)
Hierarchy - Composite Components

Abstract Semantics of Actor-Oriented Models of Computation

Actor-Oriented Models of Computation that we have implemented:

- dataflow (several variants)
- process networks
- distributed process networks
- Click (push/pull)
- continuous-time
- CSP (rendezvous)
- discrete events
- distributed discrete events
- synchronous/reactive
- time-driven (several variants)
- ...
What is an *Actor-Oriented* MoC?

Traditional component interactions:

<table>
<thead>
<tr>
<th>class name</th>
<th>data</th>
<th>methods</th>
</tr>
</thead>
</table>

What flows through an object is sequential control

Actor oriented:

<table>
<thead>
<tr>
<th>actor name</th>
<th>data (state)</th>
<th>parameters</th>
<th>ports</th>
</tr>
</thead>
</table>

What flows through an object is streams of data

Input data  Output data

Models of Computation Implemented in Ptolemy II

- CI – Push/pull component interaction
- Click – Push/pull with method invocation
- CSP – concurrent threads with rendezvous
- CT – continuous-time modeling
- DE – discrete-event systems
- DDE – distributed discrete events
- FSM – finite state machines
- DT – discrete time (cycle driven)
- Giotto – synchronous periodic
- GR – 2-D and 3-D graphics
- PN – process networks
- DPN – distributed process networks
- SDF – synchronous dataflow
- SR – synchronous/reactive
- TM – timed multitasking

Most of these are actor oriented.
Discrete Event Models

DE Director implements timed semantics using an event queue

Event source

Signal

Time line

Reactive actors

Semantics of DE Signals

A signal is a partial function:

\[ F : \mathbb{R} \times I \rightarrow T \]

Data type (set of values)

Real numbers (approximated by doubles)

Integers (allowing for simultaneous events in a signal)

Note: A signal is not a single event but all the events that flow on a path.

Lee, Berkeley 21

Lee, Berkeley 22
Subtleties: Simultaneous Events

By default, an actor produces events with the same time as the input event. But in this example, we expect (and need) for the BooleanSwitch to "see" the output of the Bernoulli in the same "firing" where it sees the event from the PoissonClock. Events with identical time stamps are also ordered, and reactions to such events follow data precedence order.

Subtleties: Feedback

Data precedence analysis has to take into account the non-strictness of this actor (that an output can be produced despite the lack of an input).
Discrete-Event Semantics

Cantor metric:
\[ d(x, y) = 1 / 2^{\tau} \]

where \( \tau \) is the earliest time where \( x \) and \( y \) differ.

Causality

Causal:
\[ d(y, y') \leq d(x, x') \]

Strictly causal:
\[ d(y, y') < d(x, x') \]

Delta causal:
\[ \exists \delta < 1, \quad d(y, y') \leq \delta d(x, x') \]

A delta-causal component is a “contraction map.”
Semantics of Composition

If the components are deterministic, the composition is deterministic.

\[ x = y \Rightarrow F(x) = x \]

Banach fixed point theorem:
- Contraction map has a unique fixed point
- Execution procedure for finding that fixed point
- Successive approximations to the fixed point

Zeno Systems

Theorem: If every directed cycle contains a delta-causal component, then the system is non-Zeno.
Extension of Discrete-Event Modeling for Wireless Sensor Nets

VisualSense extends the Ptolemy II discrete-event domain with communication between actors representing sensor nodes being mediated by a channel, which is another actor. The example at the left shows a grid of nodes that relay messages from an initiator (center) via a channel that models a low (but non-zero) probability of long range links being viable.

Distributed Discrete Event Models as Currently Implemented in Ptolemy II

DDE Director supports distributed execution and a distributed notion of time [Chandy & Misra 1979].

This is the “Chandy and Misra” style of distributed discrete events [1979], which compared to Croquet and Time Warp [Jefferson, 1985], is “conservative.”
Continuous-Time Models

Director implements a “solver” that constructs an approximation to the continuous-time behavior.

A signal has a value at all real-valued times.

Integrator used to define systems governed by ordinary differential equations.

Heterogeneous Models

Mixed Signals: DE + CT

DE model of a digital controller

CT model of mechanical system
Heterogeneous Models
Hybrid Systems: CT + FSM

The FSM director can be combined with other directors to create modal models.

Untimed Concurrency Model:
First Example: Click

Typical usage pattern:
- queues have push input, pull output.
- schedulers have pull input, push output.
- thin wrappers for hardware have push output or pull input only.
- push or pull handled by method calls

Implementation of Click with a visual syntax in Mescal (Keutzer, et al.)
Untimed Concurrency Model:
Second Example: Process Networks

This model, whose structure is due to Kahn and MacQueen, calculates integers whose prime factors are only 2, 3, and 5, with no repetitions. It uses the OrderedMerge actor, which takes two monotonically increasing input sequences and merges them into one monotonically increasing output sequence.

Actor == thread
Signal == stream
Reads block
Writes don’t

Kahn, MacQueen, 1977

PN Semantics

- A signal is a sequence of values
- Define a prefix order:
  \[ x \sqsubseteq y \]
  means that \( x \) is a prefix of \( y \).
- Actors are monotonic functions:
  \[ x \sqsubseteq y \implies F(x) \sqsubseteq F(y) \]
- Stronger condition: Actors are continuous functions (intuitively: they don’t wait forever to produce outputs).

Lee, Berkeley 36
**PN Semantics of Composition (Kahn, '74)**

If the components are deterministic, the composition is deterministic.

\[ x = y \Rightarrow F(x) = x \]

Knaster-Tarski fixed point theorem:
- Continuous function has a unique least fixed point
- Execution procedure for finding that fixed point
- Successive approximations to the fixed point

---

**Distributed Process Networks**

Transport mechanism between hosts is provided by the director. Transparently provides guaranteed delivery and ordered messages.

Created by Dominique Ragot, Thales Communications
Kepler: Extensions to Ptolemy II for Scientific Workflows

Example showing a web service wrapper (Thanks to Bertram Ludaecher, San Diego Supercomputer Center)

Synchronous Models of Computation

Director finds a value (or absent) at each “tick” of a global clock

Feedback is resolved by finding a fixed point.

Signal has a value or is absent at each tick of the “clock.”

Semantic foundation based on Kanster-Tarski fixed point theorem on Scott topologies.
Languages Based on the Synchronous Model of Computation

- Lustre (and SCADE)
- Esterel
- Signal
- Statecharts (and UML state machines)
- Argos
- …

Dataflow Models of Computation

- Computation graphs [Karp & Miller - 1966]
- Process networks [Kahn - 1974]
- Static dataflow [Dennis - 1974]
- Dynamic dataflow [Arvind, 1981]
- K-bounded loops [Culler, 1986]
- Synchronous dataflow [Lee & Messerschmitt, 1986]
- Structured dataflow [Kodosky, 1986]
- PGM: Processing Graph Method [Kaplan, 1987]
- Synchronous languages [Lustre, Signal, 1980’s]
- Well-behaved dataflow [Gao, 1992]
- Boolean dataflow [Buck and Lee, 1993]
- Multidimensional SDF [Lee, 1993]
- Cyclo-static dataflow [Lauwereins, 1994]
- Integer dataflow [Buck, 1994]
- Bounded dynamic dataflow [Lee and Parks, 1995]
- …

Many tools, software frameworks, and hardware architectures have been built to support one or more of these.
Synchronous Dataflow (SDF)  
(Lee and Messerschmitt, 1986)

SDF offers feedback, multirate, static scheduling, deadlock analysis, parallel scheduling, static memory allocation.

---

Synchronous Dataflow (SDF)  
Fixed Production/Consumption Rates

- Balance equations (one for each channel):
  \[ f_A N = f_B M \]
  - number of tokens consumed
  - number of firings per "iteration"
  - number of tokens produced

- Schedulable statically
- Get a well-defined “iteration”
- Decidable:
  - buffer memory requirements
  - deadlock

---

Lee, Berkeley 43

Lee, Berkeley 44
One Consequence of SDF Semantics:
Mobile Code that Cannot Perform Denial of Service Attacks

PushConsumer actor receives pushed data provided via CORBA, where the data is an XML model of a signal analysis algorithm.

MobileModel actor accepts an XML description of a model. It then executes that model on a stream of input data using locally defined component implementations.

SDF model has decidable semantics (termination, memory usage).

Parallel Scheduling of SDF Models

SDF is suitable for automated mapping onto parallel processors and synthesis of parallel circuits.

Many scheduling optimization problems can be formulated.
Some can be solved, too!
Scheduling Tradeoffs
(Bhattacharyya, Parks, Pino)

<table>
<thead>
<tr>
<th>Scheduling strategy</th>
<th>Code</th>
<th>Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>Minimum buffer schedule, no looping</td>
<td>13735</td>
<td>32</td>
</tr>
<tr>
<td>Minimum buffer schedule, with looping</td>
<td>9400</td>
<td>32</td>
</tr>
<tr>
<td>Worst minimum code size schedule</td>
<td>170</td>
<td>1021</td>
</tr>
<tr>
<td>Best minimum code size schedule</td>
<td>170</td>
<td>264</td>
</tr>
</tbody>
</table>

Source: Shuvra Bhattacharyya

Minimum Buffer Schedule

| Source: Shuvra Bhattacharyya   | Lee, Berkeley 48 |

Source: Shuvra Bhattacharyya
Selected Generalizations

- Multidimensional Synchronous Dataflow (1993)
  - Arcs carry multidimensional streams
  - One balance equation per dimension per arc
- Cyclo-Static Dataflow (Lauwereins, et al., 1994)
  - Periodically varying production/consumption rates
- Boolean & Integer Dataflow (1993/4)
  - Balance equations are solved symbolically
  - Permits data-dependent routing of tokens
  - Heuristic-based scheduling (undecidable)
- Dynamic Dataflow (1981-)
  - Firings scheduled at run time
  - Challenge: maintain bounded memory, deadlock freedom, liveness
  - Demand driven, data driven, and fair policies all fail
- Kahn Process Networks (1974-)
  - Replace discrete firings with process suspension
  - Challenge: maintain bounded memory, deadlock freedom, liveness
- Heterochronous Dataflow (1997)
  - Combines state machines with SDF graphs
  - Very expressive, yet decidable

Multidimensional SDF
(Lee, 1993)

- Production and consumption of \(N\)-dimensional arrays of data:
- Balance equations and scheduling policies generalize.
- Much more data parallelism is exposed.

Similar (but dynamic) multidimensional streams have been implemented in Lucid.
MDSDF Structure Exposes Fine-Grain Data Parallelism

From this, a precedence graph can be automatically constructed that reveals all the parallelism in the algorithm.

Cyclostatic Dataflow (CSDF) (Lauwereins et al., TU Leuven, 1994)

- Actors cycle through a regular production/consumption pattern.
- Balance equations become:

\[ f_A \sum_{i=0}^{R-1} N_{i \mod P} = f_B \sum_{i=0}^{R-1} M_{i \mod Q}; \quad R = \text{lcm}(P, Q) \]

\[ \text{cyclic production pattern} \]

However, such programs are extremely hard to write (and to read).
Boolean and Integer Dataflow (BDF, IDF) 
(Lee and Buck, 1993)

- Balance equations are solved symbolically in terms of unknowns that become known at run time.
- An annotated schedule is constructed with predicates guarding each action.
- Existence of such an annotated schedule is undecidable (as is deadlock & bounded memory)

\[
\begin{align*}
&f_{\text{switch}} b = f_B \\
&f_{\text{switch}} (1-b) = f_C \\
&\ldots 
\end{align*}
\]

Production rate is unknown and is represented symbolically by a variable \(b\).

Dynamic Dataflow (DDF)

- Actors have firing rules
  - Set of finite prefixes on input sequences
  - For determinism: No two such prefixes are joinable under a prefix order
  - Firing function applied to finite prefixes yield finite outputs
- Scheduling objectives:
  - Do not stop if there are executable actors
  - Execute in bounded memory if this is possible
  - Maintain determinacy if possible
- Policies that fail:
  - Data-driven execution
  - Demand-driven execution
  - Fair execution
  - Many balanced data/demand-driven strategies
- Policy that succeeds (Parks 1995):
  - Execute with bounded buffers
  - Increase bounds only when deadlock occurs

DDF, like BDF and IDF is undecidable (deadlock, bounded memory, schedule)
Undecidability (Buck '93)

- Sufficient set of actors for undecidability:
  - boolean functions on boolean tokens
  - switch and select
  - initial tokens on arcs

- Undecidable:
  - deadlock
  - bounded buffer memory
  - existence of an annotated schedule

These four parts are sufficient to build any computable function.

BDF, IDF, DDF, and PN are all undecidable in this sense. Fortunately, we can identify a large decidable subset, which we call heterochronous dataflow (HDF).

Example of a Heterochronous Dataflow Model

An actor consists of a state machine and refinements to the states that define behavior.
Heterochronous Dataflow (HDF)  
(Girault, Lee, and Lee, 1997)

- An interconnection of actors.
- An actor is either SDF or HDF.
- If HDF, then the actor has:
  - a state machine
  - a refinement for each state
  - where the refinement is an SDF or HDF actor
- Operational semantics:
  - with the state of each state machine fixed, graph is SDF
  - in the initial state, execute one complete SDF iteration
  - evaluate guards and allow state transitions
  - in the new state, execute one complete SDF iteration
- HDF is decidable
  - but complexity can be high

Related to “parameterized dataflow” of Bhattachryya and Bhattacharyya (2001).

Ptolemy II Software Architecture
Built for Extensibility

Ptolemy II packages have carefully constructed dependencies and interfaces
Polymorphic Components - Component Library  
Works Across Data Types and Domains

- Data polymorphism:
  - Add numbers (int, float, double, Complex)
  - Add strings (concatenation)
  - Add composite types (arrays, records, matrices)
  - Add user-defined types

- Behavioral polymorphism:
  - In dataflow, add when all connected inputs have data
  - In a time-triggered model, add when the clock ticks
  - In discrete-event, add when any connected input has data, and add in zero time
  - In process networks, execute an infinite loop in a thread that blocks when reading empty inputs
  - In CSP, execute an infinite loop that performs rendezvous on input or output
  - In push/pull, ports are push or pull (declared or inferred) and behave accordingly
  - In real-time CORBA, priorities are associated with ports and a dispatcher determines when to add

By not choosing among these when defining the component, we get a huge increment in component reusability. But how do we ensure that the component will work in all these circumstances?
Shared Infrastructure Modularity Mechanisms

This model illustrates the mechanisms in Ptolemy II for defining classes and subclasses with inheritance.

More Shared Infrastructure: Hierarchical Heterogeneity and Modal Models

The model shown is a hybrid control system example Ptolemy II model.
Branding

Ptolemy II configurations are Ptolemy II models that specify
- welcome window
- help menu contents
- library contents
- File->New menu contents
- default model structure
- etc.

A configuration can identify its own “brand” independent of the “Ptolemy II” name and can have more targeted objectives.

An example is HyVisual, a tool for hybrid system modeling. VisualSense is another tool for wireless sensor network modeling.

Ptolemy II Extension Points

- Define actors
- Interface to foreign tools (e.g. Python, MATLAB)
- Interface to verification tools (e.g. Chic)
- Define actor definition languages
- Define directors (and models of computation)
- Define visual editors
- Define textual syntaxes and editors
- Packaged, branded configurations

All of our “domains” are extensions built on a core infrastructure.
**Example Extension: VisualSense**

- Branded
- Customized visualization
- Customized model of computation (an extension of DE)
- Customized actor library
- Motivated some extensions to the core (e.g., classes, icon editor).

**Example Extensions: Self-Repairing Models**

Concept demonstration built together with Boeing to show how to write actors that adaptively reconstruct connections when the model structure changes.

This model is a simple example of a self-repairing model. The SmartSender actor, if not connected, will search for an unused input port to connect to and will establish a connection.

If you have Java code installed, look inside the SmartSender to see how this is realized. Or get documentation for a more detailed explanation.

Author: Edward A. Lee
Example Extensions
Python Actors and Cal Actors

Cal is an experimental language for defining actors that is analyzable for key behavioral properties.

This model demonstrates the use of function closures inside a CAL actor.

The PrimeSieve actor uses nested function closures to realize the Sieve of Eratosthenes, a method for finding prime numbers. Its state variable, "filter," contains the current filter function. If it is "false" a new prime number has been found, and a new filter function will be generated.

The PrimeSieve actor expects an ascending sequence of natural numbers, starting from 2, as input.

Example Extensions
Using Models to Control Models

This model illustrates the use of a "run composite actor" component. That component contains another Picolak f model. Each time it fires, it performs a complete execution of that other Picolak f model, rather than just one firing as would be typical of a composite actor.

This model generates Lissajous figures, which are plots of one sinusoid vs. another. On each execution, it generates one figure.

This is an example of a "higher-order component," or an actor that references one or more other actors.
Examples of Extensions
Mobile Models

Model-based distributed task management:

PushConsumer actor receives pushed data provided via CORBA, where the data is an XML model of a signal analysis algorithm.

MobileModel actor accepts a StringToken containing an XML description of a model. It then executes that model on a stream of input data.

Examples of Extensions
Hooks to Verification Tools

New component interfaces to Chic verification tool

Authors:
Arindam Chakrabarti
Eleftherios Matsikoudis

Authors:
Yang Zhao
Steve Neuendorffer
Xiaojun Liu

Lee, Berkeley 69

Lee, Berkeley 70
Examples of Extensions
Hooks to Verification Tools

Synchronous assume/guarantee interface specification for Block1

Examples of Extensions
Hooks to Verification Tools

Lee, Berkeley 71

Lee, Berkeley 72
Conclusion

- Threads suck
- There are many alternative concurrent MoCs
- The ones you know are the tip of the iceberg
- Ptolemy II is a lab for experimenting with them
- Specializing MoCs can be useful
- Mixing specialized MoCs can be useful.