

EECS20n, Quiz 1, 1/30/04

The quiz will take 10 minutes. Write your response on the sheet.

Please print your name and lab time here:

Last Name _____ First _____ Lab time _____

Indicate whether the following statements are **true** or **false**. There will be no partial credit, so please consider your answer carefully. Put a box around your answer.

1. The sets $\{0, 1, 2, \dots\}$ and $\{1, 2, 3, \dots\}$ have the same cardinality.
2. The sets $\{0, 1, 2, \dots\}$ and $[0, 1]$ have the same cardinality.
3. $\exists y \in \mathit{Reals} \forall x \in \mathit{Reals} \ y < x$.
4. $\forall x \in \mathit{Reals} \exists y \in \mathit{Reals} \ y < x$.
5. Consider the function x where $\forall t \in \mathit{Reals}, x(t) = 2$. Then $x \in [\mathit{Reals} \rightarrow \mathit{Reals}]$.
6. Let $f: \mathit{Reals} \rightarrow \mathit{Reals}$ and $g: \mathit{Reals} \rightarrow \mathit{Reals}$. Define the functions $f + g$ by $\forall x \in \mathit{Reals}, (f + g)(x) = f(x) + g(x)$, and $g \circ f$ by $\forall x \in \mathit{Reals}, (g \circ f)(x) = f(g(x))$. Then
$$f + g = g + f$$
$$f \circ g = g \circ f$$
7. There is a function $f: \{1, 2\} \rightarrow \{a, b\}$ with $\mathit{graph}(f) = \{(1, a), (2, a)\}$.
8. Let $f: X \rightarrow Y$. Then $\mathit{graph}(f) \subset X \times Y$.
9. Let $G \subset X \times Y$. There exists a function f such that $\mathit{graph}(f) = G$.