# EECS 20. Midterm No. 2, April 9, 1999. <br> Please use these sheets for your answer. Add extra pages if necessary and staple them to these sheets. Write clearly and put a box around your answer, and show your work. 

Print your name below

Last Name $\qquad$ First

Problem 1:
Problem 2:
Problem 3:
Problem 4:
Total:

1. 30 points Consider an LTI system with impulse response $h$ given by

$$
\forall n \in \text { Ints }, \quad h(n)=\delta(n)+\delta(n-1),
$$

where $\delta$ is the Kronecker delta function. Let $H$ denote the frequency response of this system. Suppose that two copies of this system are connected in cascade, meaning that the output of the first one feeds the input of the second.
(a) Find the impulse response $g$ of the cascade system.
(b) Give the frequency response $G$ of the cascade system in terms of $H$.
(c) Find $H$ and $G$ as functions of $\omega$, frequency in radians/sample.
2. 30 points Consider an LTI system $L$ with impulse response $h$ given by

$$
\forall n \in \text { Ints }, \quad h(n)=\delta(n+2)+\delta(n-2),
$$

where $\delta$ is the Kronecker delta function.
(a) Find the frequency response $H$ as a function of $\omega$, frequency in radians per sample.
(b) Find one value of $\omega$ such that if the input is the signal $x$ where

$$
\forall n \in \text { Ints, } \quad x(n)=\cos (\omega n),
$$

then the output $y$ will be zero, i.e.

$$
\forall n \in \text { Ints }, \quad y(n)=0 .
$$

(c) Consider another filter with impulse response

$$
h_{2}(n)=\delta(n)+\delta(n-4) .
$$

Show that you can use the result of part (a) to quickly and easily find the frequency response of this version. (It is important the you make the connection with part (a), not just that you find the frequency response of the new filter).
3. $\mathbf{2 0}$ points Let $x$ be a continuous-time signal given by

$$
\forall t \in \text { Reals }, \quad x(t)=\sin (2 \pi 3000 t)+\sin (2 \pi 5000 t) .
$$

(a) For what values of $T$ will it be true that

$$
x=\text { IdealInterpolator }_{T}\left(\operatorname{Sampler}_{T}(x)\right) ?
$$

(b) Find the signal $y$ given by

$$
y=\text { IdealInterpolator }_{T}\left(\operatorname{Sampler}_{T}(x)\right)
$$

where $T=1 / 8000$ is the sampling interval. Hint: Do not use the sinc function definition of IdealInterpolator $_{T}$. Consider instead the aliases of the two sinusoidal components.
4. 20 points A certain device is controlled via a keyboard that has only the alphabetic keys, A through Z. Assume that you can only press one key at a time (unlike a real computer keyboard). A portion of the specification this device says:

To shut down the device, the user should hit keys "A", "B", and "C" in sequence, one at a time.

The designer of the device uses a state machine to get the desired behavior, and defines the state machine with the following table:

| state | next state under input |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | A | B | C | $\mathrm{D}-\mathrm{Z}$ |
| state1 | state 2 |  |  |  |
| state2 |  | state3 |  | state1 |
| state3 |  |  | stop | state1 |
| stop |  |  |  |  |

The start state is state1. The blank entries indicate that the state machine stays in the same state. There is no output from this state machine. Notice that the response to the whole set of keys D through Z is given in a single column of the table, for compactness.
(a) Sketch and label the state transition diagram corresponding to the above table. Be sure your diagram specifies all aspects of the behavior. In particular, show "else" transitions (if any) explicitly.
(b) The table has a bug in it. Its behavior does not quite match the specification. Identify the bug; in particular, give a sequence of inputs that illustrates the bug, and give a state transition table that corrects the bug.

